Semester Courses of M.A/M.Sc. Mathematics Based on CBCS

The course of M.A/M.Sc. (Mathematics) will be spread in two years - Previous and Final. Each of which will have two semester examinations and therefore will be four semester examinations.

M.A./M.Sc. Previous (Mathematics)
(Effective from Session 2019-2020)

The M.A./M.Sc. Previous (Mathematics) examination will consist of two semesters, called as first and second semesters. Their examinations will be held in the months of December and May respectively. In each of these semester examinations, there will be five compulsory papers. Each paper will be of three hours duration and of 5 credit (maximum marks 70), except where stated otherwise. There will be 30% internal evaluation in each paper based on:

1. Attendance 10 Marks
2. Class Test/ Assignment 10 Marks
3. Seminar 10 Marks

Format of the Question Paper:-

There will be one compulsory question consisting of 4 parts of short answer type questions based on the whole course, out of which all parts will have to be answered. Besides this, there will be 8 questions from four units (**two from each unit**) ,out of which 4 questions will have to be answered (**one from each unit**). Thus in all, 5 questions will have to be attempted and 9 questions will have to be set. All questions will carry equal marks, except stated otherwise.

First Semester

S.No.	Paper	Course Code	Paper Title
1	Paper I	MAT-101	Groups and Canonical Forms
2	Paper II	MAT-102	Topology
3	Paper III	MAT-103	Differential and Integral Equations
4	Paper IV	MAT-104	Complex Analysis
5	Paper V	MAT-105	Real Analysis

Second Semester

S.No.	Paper	Course Code	Paper Title
1	Paper I	MAT-201	Fields and Modules
2	Paper II	MAT-202	Differential Geometry of Manifolds
3	Paper III	MAT-203	Partial Differential Equations
4	Paper IV	MAT-204	Operations Research
5	Paper V	MAT-205	Fluid Dynamics

M.A./ M.Sc. Final (Mathematics)

(Effective from session 2020-2021)

The M.A./M.Sc. Final (Mathematics) will consist of two semesters, called as third and fourth semesters. Their examinations will be held in the months of December and May respectively. In each of these semester examinations there will be three compulsory papers and two elective papers to be selected from each group of optional papers. Each paper will be of three hours duration and of 5 credit (maximum marks 70), except where stated otherwise. There will be 30% internal evaluation in each paper based on:

1. Attendance 10 Marks
2. Class Test/ Assignment 10 Marks
3. Seminar 10 Marks

Format of the Question Paper.

There will be one compulsory question consisting of 4 parts of short answer type questions based on the whole course, out of which all parts will have to be answered. Besides this, there will be 8 questions from four units (**two from each unit**) ,out of which 4 questions will have to be answered (**one from each unit**). Thus in all, 5 questions will have to be attempted and 9 questions will have to be set. All questions will carry equal marks, except stated otherwise.

Third Semester

S.No.	Paper	Course Code	Paper Title
		Core Papers	
1	Paper I	MAT-301	Number Theory
2	Paper II	MAT-302	Banach Spaces
3	Paper III	MAT-303	Dynamics of Rigid Bodies
	Paper IV	**Elective Papers** (Opt any one)	
4		MAT-304	Fourier Analysis and Summability Theory
5		MAT-305	General Relativity and Gravitation
6		MAT-306	Numerical Solution of Differential Equations
7		MAT-307	Advanced Topology
8		MAT-308	Hydrodynamics
	Paper V	**Elective Papers** (Opt any one)	
9		MAT-309	Discrete Mathematics
10		MAT-310	Mathematical Modelling
11		MAT-311	Complex Manifolds
12		MAT-312	Riemannian Geometry
13		MAT-313	Magneto Hydrodynamics

Fourth Semester

S.No.	Paper	Course Code	Paper Title
Core Papers			
1	Paper I	MAT-401	Measure Theory
2	Paper II	MAT-402	Hilbert Spaces
3	Paper III	MAT-403	Analytical Dynamics
	Paper IV	**Elective Papers** (Opt any one)	
4		MAT-404	Fixed Point Theory and its Application
5		MAT-405	Cosmology
6		MAT-406	Wavelet Analysis
7		MAT-407	Hydro Statics
8		MAT-408	Mathematics for Humanities (Not for Mathematics Students)
	Paper V	**Elective Papers** (Opt any one)	
9		MAT-409	Information Theory
10		MAT-410	Bio Mathematics
11		MAT-411	Contact Manifolds
12		MAT-412	Finsler Geometry
13		MAT-413	Mathematics for Life Sciences

M.A/M.Sc. First Semester Based on CBCS (Mathematics)

Paper I- Groups and Canonical Form (MAT-101) **Total Credit-5**

Unit-I

Groups **:** Conjugacy relation. Normaliser of an element, Class equation of a finite group, Center of a group, Fundamental theorems on isomorphism of groups, Automorphisms, Inner automorphism.

Unit-II

Maximal subgroups, Commutator subgroups, Composition series, Examples of Composition series and normal series. Jordan-Holder theorem, Solvable groups, Solvable subgroups, Nilpotent groups.

Unit-III

External and internal direct product of groups, Cauchy's theorem for finite group, Cauchy's theorem for abelian group, Groups of order p^2 *and* pq, Sylow's p subgroups, Sylow's first, second and third theorems. Application of Sylow's theorems to find the number of Sylow's p subgroups of a finite groups.

Unit-IV

Canonical forms: Similarity of linear transformations, Invariant subspaces, Reduction to triangular forms, Nilpotent transformations, Index of nilpotency, Invariants of a nilpotent transformation, The primary decomposition theorem, Jordan blocks and Jordan forms.

Books Recommended:-

1. I.N. Herstein : Topics in Algebra, Wiley Eastern Ltd., New Delhi.

2. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul : Basic Abstract Algebra (Second Edition), Cambridge University Press, Indian Edition.

3. Surjeet Singh and Qazi Zameeruddin: Modern Algebra, Vikas Publishing House. Pvt. Ltd.

4. K.B. Datta : Matrix and Linear Algebra, Prentice Hall of India Pvt. Ltd., New Delhi,.

5. S. Kumaresan : Linear Algebra, A Geometric Approach, Prentice Hall of India.

6. A.R. Vasishtha & A.K. Vasishtha : Modern Algebra, Krishna Prakashan Media (P) Ltd., Meerut .

7. H.K.Pathak: Abstract Algebra, Shiksha Sahitya Prakashan.

Paper II-Topology (MAT-102) **Total Credit-5**

Unit-1

Definition and examples of topological spaces. Closed sets. Closure. Dense subsets. Neighbourhoods. Interior, exterior and boundary. Accumulation points and derived sets. Bases and sub-bases. Subspaces and relative topology. Neighbourhood Systems.

Unit-II

Continuous functions and homeomorphism. First and second countable spaces. Lindelof's theorems. Separable spaces. Second Countability and Separability.

Unit-III

Separation axioms T0,T1,T2,T3,T4; their characterizations and basic properties. Urysohn Lemma. Tietz extention theorem.

Unit-IV

Compact sets and their properties. Finite intersection property, Bolzano Weierstrass property. Continuous functions and compactness, Sequential compactness, countable compactness and their comparison. One point compactification. Connected spaces. Connectedness on the real line. Components. Locally connected Spaces.

Books Recommended:-

1. George F. Simmons : Introduction to Topology and Modern Analysis, Mc Graw-Hill Book Company.
2. J.L. Kelley : General Topology, Van Nostrand, Reinhold Co., New York.
3. K.D. Joshi: Introduction to General Topology, Wiley Eastern Ltd.
4. James R Munkres : Topology, Prentice Hall of India Pvt. Ltd., New Delhi.
5. Willard: General Topology Addison-Wesley, Reading.

Paper III-Differential and Integral Equations (MAT-103) Total Credit-5

Unit I:

Solution of Differential Equations in ascending and descending power series, Hypergeometric Differential Equations, Papperitz symbol, Pochhammer symbol, Hypergeometric Function, Solution of Gauss's Hypergeometric Differential Equation, Differentiation of Hypergeometric Functions.

Unit II:

Legendre's Differential Equation, Legendre's Functions, Generating Function for $P_{n,}$ Laplace Definite Integrals for $P_n(x)$, Orthogonal properties of Legendre's Polynomials, Recurrence Formulae, Beltrami Result, Christoffel's Expansion and Summation formulae, Rodrigue's Formula for $P_n(x)$.

Bessel's Differential Equation, Bessel's Functions, Generating Function for $J_n(x)$, Differential Equations Reducible to Bessel's Differential Equations, Orthogonality of Bessel's Functions.

Unit III:

Integral Equations, Linear Integral Equations, Types of Linear Integral Equations, Types of Kernels, Conversion of differential equations to integral equations, L_2 kernels and L_2 Functions, Eigen values and eigen functions, Solution of Volterra Integral Equations by Successive Approximations and Successive Substitution Methods.

Unit IV:

Fredholm Integral Equations of First and Second kinds, Solution of Fredholm Integral Equations by Successive Approximations and Successive Substitution Methods, Neumann Series, Volterra solution of Fredholm Integral Equation of second kind, Reduction of Volterra Integral Equation into differential equation, Reduction of Volterra Integral Equation of first kind into Volterra Integral Equation of second kind.

Books Recommended:-

1. Differential and Integral Equations by B.P. Parashar
2. Series Solution and Special Functions by V. S. Verma
3. Fundamentals of Integral Equations by V. S. Verma
4. Integral Equations and Boundary Value Problems by M D Raisinghania
5. Integral Equations by Shanti Swarup and Shiv Raj Singh
6. Linear Integral Equations by R. P. Kanwal

Paper IV-Complex Analysis (MAT-104) **Total Credit-5**

Unit I:

Conformal Mapping, Mobius (Bilinear) transformations: involving circles and half-planes, fixed point, cross ratio, Transformations $w=z^2$, $w = \tan^2 (z/2)$,Univalent function and its properties. Many valued functions and its properties.

Unit II:

Power series and its convergence. Analyticity of power series, singularity of power series, Gamma function. Zeta Function

Unit III:

Maximum-modulus theorem. Schwarz's lemma. Hadamard's three-circles theorem. Borel-Cartheodory theorem. Pharagmen- Lindelof theorem.

Unit IV:

Analytic continuation. Uniqueness of analytic continuation. Power series method of analytic continuation. Natural boundary.

Books Recommended:-

1. E.C. Titchmarsh: Theory of Functions, Oxford University Press, London.
2. Mark J. Ablowitz and A.S. Fokas: Complex Variables: Introduction and Applications, Cambridge University Press, South Asian Edition, 1998.
3. R.V. Churchill & J.W. Brown. Complex Variables and Applications, 5th Edition McGraw-Hill, New York, 1990.
4. Shanti Narayan: Theory of Functions of a Complex Variable, S. Chand & Co., New Delhi.
5. S. Ponnusamy, Foundation of Complex Analysis, Narosa Publication

Paper V-Real Analysis (MAT-105) **Total Credit 5**

Unit I:

Functions of Bounded Variation and some properties of function of bounded variation, Lipschitz condition and function.Variation function and The Jordan Decomposition theorem.

Unit II:

Definition and Existence of Riemann- Stieltjes integrals. Properties of the integral, integration and differentiation, the first and second mean value theorem, the fundamental theorem of integral calculus, change of variable and Integration by parts forRiemann- Stieltjes. Relation between Riemann and Riemann- Stieltjes integral.Riemann- Stieltjes integrals and bounded variation.

Unit III:

Sequencesof functions of real numbers. Pointwise convergence and uniform convergence. Cauchy Criterion of uniform convergence, M_n test, Weierstrass M- test, everywhere continuous but nowhere differentiable functions. Dini'scriterion of uniform convergence. Uniform convergence and continuity. Continuity of limit function. Uniform convergence and Riemann stieltjes integration,Uniform convergence and differentiation.

Unit IV:

Abel's and Dirichlet's tests for uniform convergence. Connections between Riemann- Stieltjes integrals, uniform convergence and bounded variation. Curves, Rectifiable curves, Additive and Continuity properties of arc length. Rearrangements of terms of a series, Dirichlet's and Riemann's theorem. Power series, uniqueness theorem for power series, Abel's and Tauber's theorem for power series.

Books Recommended:-

1. Walter Rudin: Principles of Mathematical Analysis (3rd edition), McGraw-Hill, Kogakusha, 1976 International Student Edition.

2. H. L. Royden: Real Analysis, Macmillan Pub. Co. Inc. New York, 4th Edition, 1993.

3. Richard Johnson Baugh: Foundation of Mathematical Analysis.

4. H.K.Pathak: Real Analysis, Shiksha Sahitya Prakashan.

5. Apostol:Mathematical Analysis, Narosa Publishing House.

M.A/M.Sc. Second Semester Based on CBCS (Mathematics)

Paper I - Fields and Modules (MAT-201) **Total Credit-5**

Unit-I

Field theory: Extension Fields. Algebraic and transcendental extensions. Splitting Field. Separable and inseparable extensions.

Unit-II

Normal extension. Perfect Fields. Finite Fields. Antomorphisms of extensions.

Unit-III

Galois group. Fundamental theorem of Galois theory. Construction with ruler and compass. Solution of polynomial equations by radicals. Insolvability of the general equation of degree 5 by radicals.

Unit-IV

Modules, Cyclic modules. Simple modules . Semi-simple modules. Schuler?s lemma. Free modules. Noetherian and artinian modules. Hilbert basis theorem.

Recommended Books:

1. I.N. Herstein : Topics in Algebra, Wiley Eastern Ltd., New Delhi.
2. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul : Basic Abstract Algebra (Second Edition), Cambridge University Press, Indian Edition.
3. Surjeet Singh and Qazi Zameeruddin: Modern Algebra, Vikas Publishing House. Pvt. Ltd.
4. K.B. Datta : Matrix and Linear Algebra, Prentice Hall of India Pvt. Ltd., New Delhi.
5. S. Kumaresan : Linear Algebra, A Geometric Approach, Prentice Hall of India.
6. A.R. Vasishtha & A.K. Vasishtha : Modern Algebra, Krishna Prakashan Media (P) Ltd., Meerut .
7. H.K.Pathak: Abstract Algebra, Shiksha Sahitya Prakashan.

Paper II -Differential Geometry of Manifolds (MAT-202) **Total Credit- 5**

Unit- I

Tensor Algebra: Contravariant and covariant vector. Tensor product of vector spaces, tensor, contravariant, covariant and mixed tensor of second order. Tensor of type (r, s), tensor product of tensors. Algebraic operations, symmetric and skew symmetric tensors, contraction.

Unit- II

Definition and examples of differentiable manifold. Differentiable functions. Differentiable curves .Tangent space .Vector fields. Lie bracket. Invariant view point of connections. Covariant differentiation.

Unit- III

Torsion. Curvature. Parallelism. Difference tensor of two connections. Lie derivative. Riemannian Manifold. Riemannian connection. Riemannian curvature tensor and Ricci tensor. Idenitities of Bianchi. Sectional curvature and Schur's theorem.

Unit -IV

Exterior product of two vectors. Exterior algebra of order r .Exterior derivative .Cartans's structural equations.Submanifolds and Hypersurfaces. Normals. Gauss's formula. Weingarten equations.

Books Recommended:

1. R. S. Mishra, A Course in Tensors with Applications to Riemanian Geometry, Pothishala, Allahabad, 1965.

2. Y. Matsushima, Differentiable Manifolds, Marcel Dekker, 1972.

3. B. B. Sinha, An Introduction to Modern Differential Geometry, KalyaniPrakashan, New Delhi, 1982.

4. Y. Talpiert, Differential Geometry with applications to Mechanics and Physics, Marcel Dekkar Inc. 2001.

5. N.J. Hicks, Notes on Differential Geometry, D. Van Nostrand Inc., 1965.

6. U.C.De and A.A.Shaaikh, Differential Geometry of Manifolds, Narosa Publishing House, New Delhi 2007.

7. K.S.Amur ,D.J.Shetty and C.S.Bagewadi , An Introduction to Differential Geometry , Narosa Publishing House, New Delhi 2010.

8.S.Shahshahani, An Introductory Course on Differentiable Manifolds, Dover Publication ,Inc. New York ,2016.

Paper III- Partial Differential Equations (MAT-203) **Total Credit-5**

Unit- I

Origin of first order partial differential equations, Lagrange's solution of first order linear partial differential equation.

Unit- II

Non-linear partial differential equations of the first order, Cauchy's method of characteristics, Charpit's method and Jacobi's method.

Unit- III

Origin of second order partial differential equations, Higher order partial differential equations with constant coefficients, Equations with variable coefficients, Classification of second order partial differential equations, Canonical forms.

Unit- IV

Solution of non-linear second order partial differential equations by Monge's method, Method of separation of variables for solving Laplace, wave and diffusion equations.

Books Recommended:

1. V.S.Verma : A Text Book of Partial Differential Equations
2. A.R. Forsyth : A Treatise on Differential Equations
3. I.N. Sneddon : Elements of Partial Differential Equations.
4. LC Evans, Partial Differential Equations, AMS, 1998
5. M.D. Rai Singhania: Advanced Differential Equations, S. Chand.
6. Donald Greenspan: Introduction to Partial Differential Equations, Dover publications, New York.
7. Peter V. O'Neil: Beginning Partial Differential Equations, Wiley.

Paper IV- Operations Research (MAT-204) **Total Credit-5**

Unit-I

Inventory Control: Introduction, Classification of Inventory, Economic parameter associated with inventory problems, Deterministic and Probabilistic models with without lead time.

Unit-II

Sequencing Problems :Assumptions for seqnencing problem. Processing n jobs on two machines, n jobs on three machines, 2 jobs on m machines, Problem of Replacement, Individuals and Group replacement policies.

Unit-III

Network analysis: Basic concepts and definition. Network drawing and analysis Critical path method. Labelling method. Methods based on time estimates to find critical path. Concept of slack and float. Resource levelling and time-cost trade-off analysis. Time-cost optimization procedure. Project crashing. PERT. Requirements for application of PERT technique. Practical limitations in using PERT. Diffferences in PERT and CPM.

Unit-IV

Non-Linear Programming:Introduction and defintions. Formulation of non-Linear programming problems, General non-linear programming problems. Kuhn-Tucker conditions, Lagrangian Method, Constrained optimization with equality constraints. Constrained optimization with inequality constaints. Saddle point problems Saddle points and NLPP. Wolfe's and Beale's method to solve Quadratic Progamming problem.

Books Recommended:

1. S.D. Sharma: Operations Research, Kedar Nath Ram Nath & Company.
2. S.S. Rao: Optimization Theory and Applications, Wiley Eastern Ltd., New Delhi.
3. J.K. Sharma: Operations Research – Theory and Applications, Macmillan India Ltd.
4. H.A. Taha: Operations Research – An Introduction, Macmillan Publishing Co., Inc., New York.
5. Kanti Swarup, P.K. Gupta, Man Mohan: Operations Research, Sultan Chand and sons, New Delhi.
6. B.S. Goel, S.K. Mittal: Operations Research, Pragati Prakashan, Meerut.
7. P.K. Gupta, D.S. Hira: Operatons Research – An Introduction, S. Chand & CompanyLtd., New Delhi.

Paper -V Fluid Dynamics (MAT-205) **Total credit-5**

Unit-I

Fluid motion, Lagrangian and Eulerian methods, Stream Lines. Path lines and streak lines. Velocity potential. Vorticity Vector. Irrotational and rotational motions. Boundary surfaces. Euler's and Lagrange's Equation of continuity. Forms of equation of continuity in different coordinate system. Symmetrical forms of equation of continuity. Lagrange's and Euler's equations of motion. Pressure equation. Bernoulli's theorem.

Unit-II

Newton's law of viscosity. Kinds of fluids. Nature of stress. Stress components in a real fluid. Symmetry of stress tensor. Transformation of stress components. Stress invariants. Relations between Cartesian components of stress. Rate of strain quadric. Principal stresses. Stoke's law of viscosity. Relations between stress and rate of strain.

Unit-III

Navier-Stokes equations of motion, Steady viscous flow between parallel planes. Laminar flow between parallel plates(walls). Plane Couette flow. Plane Poiseuille flow. Hagen-Poiseuille flow. Steady flow through a tubes of uniform circular cross-sections.

Unit-IV

Steady flow between concentric rotating cylinders. Laminar steady flow between two coaxial circular cylinders. Diffusion of vorticity. Energy dissipation due to viscosity. Reynolds number. Significance of Reynolds number.

Books Recommended:-

1. J.K. Goyal and K.P. Gupta: Fluid Dynamics, Pragati Prakashan, Meerut, 2017
2. N. Curle and H. J. Davis: Modern Fluid Dynamics, D. Van Nostrand Company Ltd. London, 1968.
3. G.K. Batchelor: An Introduction to Fluid Dynamics, Cambridge University Press, Cambridge, 2000.

M.A/M.Sc. Third Semester Based on CBCS (Mathematics)

Paper-I Number Theory (MAT-301) **Total Credit-5**

Unit-I

Divisibility: Some basic terms and properties, Division algorithm, Common divisor, Greatest common divisor (gcd), Theorems on gcd, Euclid's lemma, Relatively prime, Euclidian Algorithm, least common multiple (lcm), Theorems on lcm, Fundamental theorem of arithmetic, Euclid's theorem.

Unit-II

Congruences: Theorems of congruences, Residue and complete residue system, Reduced residue system, Euler's ϕ function, Euler's theorem, Fermat's theorem, Wilson theorem, Converse of Wilson theorem, Solutions of congruences, Degree of congruence, Chinese remainder theorem, Method of solution of congruences.

Unit-III

Prime modules and Cryptography: Prime modules, Power residues, Number theory from algebraic point of view, Introduction of cryptography, Some simple cryptosystems, Enciphering matrices.

Unit-IV

Quadratic reciprocity: Quadratic residues, Gauss lemma, Gaussian reciprocity law, Jacobi symbol, Greatest integer function, Arithmetic function, Multiplication of arithmetic functions, Moebius function, Moebius inversion formula, Converse of Moebius inversion formula, Recurrence functions, Fibonacci numbers

Books recommended:

1. Niven and Zuckermann: An Introduction to the theory of numbers, Wiley Eastern Ltd.
2. Ireland & Rosen, A Classical Introduction to Modern Number Theory, Springer
3. Tom Apostol, Introduction to Analytic Number theory, Narosa Publications, New Delhi
4. Delfs, H., Knebl, H., Introduction to Cryptography, Springer.
5. Koblitz, N., Algebraic Aspects of Cryptography, Springer.
6. Serre, J.P., A Course in Arithmetic, Springer.
7. Cassels, J.W.S., Frolich, A., Algebraic Number Theory, Cambridge

Paper II -Banach Spaces (MAT-302) **Total Credit-5**

Unit I:

Normed linear spaces, Banach spaces, their examples including R^n ,C^n , l_p (n), $1 \leq p < \infty$, c0 ,c, l_p , $1 \leq p < \infty$, P [a,b], C[a,b]. Joint continuity of addition and scalar multiplication. Summable sequences and completeness. Subspaces, Quotient spaces of normed linear space and its completeness.

Unit II:

Continuous and bounded linear operators and their basic properties. Normed linear space of bounded linear operators and its completeness. Equivalent norms. Finite dimensional normed spaces and compactness.

Unit III:

Isometric isomorphism, Topological isomorphism. Riesz Theorem, Open mapping theorem and its simple consequences. Product normed space. Closed graph theorem. Uniform boundedness. Banach-Steinhaus theorem. Adjoint of bounded Linear operators.

Unit IV:

Bounded linear functionals Dual spaces. Form of dual spaces $(R^{n)}$*, (C^n)*,c_o^*, l_1^* , l_p^*, $1<p<\infty$. Hahn- Banach theorem for real and complex normed linear spaces and its simple consequences. Embedding and Reflexivity. (1credit)

Books Recommended:

1. P.K. Jain, O.P. Ahuja and K. Ahmad: Functional Analysis, New Age International (P) Ltd. and Wiley Eastern Ltd., New Delhi, 1997.
2. B. Choudhary and S. Nanda: Functional Analysis with Applications, Wiley Eastern Ltd., 1989.
3. I.J Maddox: Functional Analysis, Cambridge University Press (1970).
4. B.V.Limaye: Functional Analysis,New Age International Publications, New Delhi.
5. K. Chandrashekhara Rao. Functional Analysis, Narosa Publishing House, New Delhi
6. W.Rudin: Functional Analysis, TMH, New Delhi H.K.Pathak: Functional Analysis with Applications, Siksha Sahitya Prakashan, Merrut

Paper III- Dynamics of Rigid Bodies (MAT-303) **Total Credit-5**

Unit-I

Rigid Body, properties of rigid body and its motion, impressed and effective forces, finite and impulsive forces, D' Alembert's principle, general equation of motion of a rigid body from D'Alembert's principle, motion of the centre of inertia, motion about centre of inertia, Application of D'Alembert's principle to impulsive forces,

Unit-II

Motion about a fixed axis: moment of effective forces about the axis of rotation, kinetic energy, equation of motion, compound pendulum, centre of suspension, minimum time of oscillation of compound pendulum, reaction of the axis of rotation, motion about a fixed axis (impulsive forces).

Unit-III

Motion of a rigid body in two dimensions under finite forces: Equation of motion, Kinetic energy, moment of momentum in two dimensions, motion of solid sphere down an inclined plane, slipping of rods, motion of solid sphere down an inclined plane when rolling and sliding are combined, Motion of circular disc, determination of sliding at the point of contact during relative motion of two bodies in contact, motion of one sphere on the other which is fixed, motion of solid cylinder inside a hollow cylinder, motion of one body on the other when the lower body is free to turn about its axis, motion of one body on another when both bodies are free to move.

Unit-IV

Motion in two dimensions under impulsive forces, Moving axes and the fixed axes, Rotation of a vector in 2D and 3D space, motion of a particle in rotating space, motion of a rigid body in rotating frame, effects of earth rotation, free particle motion relative to earth, effects of coriolis force on some natural events, Eulerian approach to rigid body motion, Euler dynamical equations of motion for finite and impulsive forces, Kinetic energy of a rigid body about a fixed point, Eulerian angles and geometrical relations, instantaneous axis of rotation, invariable line, locus of invariable line.

Books Recommended:-

1. S.L. Loney: An Elementary Treatise on the Dynamics of a Particle and of Rigid Bodies, Macmillan India Ltd., 1982.
2. A.S. Ramsey: Dynamics Part-II, The English Language Book Society and Cambridge University Press, 1972.
3. J.L. Synge and B.A. Griffith: Principles of Mechanics, McGraw Hill International Book Company, 1982.
4. P.P. Gupta, G.S. Malik: Rigid Dynamics I, Krishna Prakashan Media (P) Ltd.2008.
5. Naveen Kumar, Generalized Motion of Rigid Body, Narosa Publishing House, New Delhi.

Paper IV - Fourier Analysis and summability Theory (MAT-304) **Total Credit-5**

Unit-I

Convergence problem, Dirichlet's integral, Riemann-Lebesgue Theorem,Convergence tests , Dini's, Jordan's, de la Vallee-Poussin's tests and theirinter-relations. Summation of series by arithmetic means

Unit-II

summability of Fourier series, Fejer's theorem, Weierstrass's approximation theorem,Almost everywhere summability, The Fej_er-Lebesgue theorem, A continuous fuction with a divergent Fourier series, Order of partial sums, Integration of Fourier series, Convergent trigonometric series need not be a Fourier series, Parseval's theorem.

Unit—III

Functions of the class L2: Bessel's inequality, Parseval's theorem for continuous functions, The Riesz- Fischer theorem, Properties of Fourier coefficients, Uniqueness of trigonometric series, Cantor's lemma, Riemann's First and second theorems.

Unit-IV

Special methods of summation: Norlund means, Regularity and Consistency of Norlund means, Inclusion, Equivalence, Euler's means, Abelian means, Riesz's typical means. Arithmetic means: Holder's means, simples theorems concerning Holder summability, Cesaro means, means of non-integral orders, simple theorems concerning Cesaro summability , Cesaro and Abel summability, Cesaro means as Norlund means, Tauberian theorems for Cesaro summability.

Recommended Books:

1. E.C. Titchmarsh: A Theory of Functions, Oxford University Press, 1939.
2. A Zygmund: Trigonometric series Vol. I, The University Press, Cambridge 1959
3. G. H. Hardy: Divergent series, The Clarendon Press, Oxford, 1949.

Paper IV General Relativity and Gravitation (MAT-305) Total Credit-5

Unit-1

Space time, Curved Space time, Riemannian metric, Riemannian curvature tensor, Conformal curvature tensor, Parallel transport and Geodesic, Geodesic Deviation., Lie derivative.

Unit-II

Introduction to General Relativity, Principal of Equivalence, Principal of General covariance, Mach's Principle, Newtonian approximation of equation of motion. Einstein's field equation, Gravitational field in empty space

Unit-III

Schwarzschild exterior solution, Singularities in Schwarzschild line element,Kruskal-Szekers coordinate, Isotropic form of Schwarzschild exterior line element, Birkhoff's theorem

Unit-IV

Planetary orbits. The advanced of perihelion, Bending of light rays in gravitational field, The gravitational red-shift of spectral lines, Kepler's Law in General Relativity, Energy momentum tensor, Formula for energy momentum tensor for perfect fluid, Vaidya metric.

Books Recommended:-

1. K. D. Krori : Fundamentals of Special and General Relativity; PHI Publication, 2010.
2. S. R. Roy and Raj Bali : Theory of Relativity; Jaipur Publishing House, 2008.
3. Steven Weinberg : Gravitation and Cosmology : Principles and applications of General Relativity; Wiley Publ.,2005.
4. J. V. Narlikar : An Introductions to Relativity; Cambridge University Press, 2010.
5. I.B. Khriplovich : General Relativity; Springer Science + business media, 2005.

Paper IV - Numerical Solution of Differential Equations (MAT-306) Total Credit-5

Unit-I

Numerical Solution of parabolic partial differential equations (PDE) in one space: two and three levels explicit and implicit differences schemes. Convergence and stability analysis.

Unit-II

Numerical solution parabolic PDE of second order on two spaces dimension: Implicit methods, alternating direction implicit (ADI) methods. Non-linear initial BVP (boundary valued problems). Differences schemes for parabolic PDE in spherical and cylindrical coordinate systems in one dimension.

Unit-III

Numerical solution of hyperbolic PDE in one and two spaces dimension: explicit and implicit schemes: ADI methods. Differences schemes for first order equations, Numerical solutions of elliptical equations

Unit-IV

Approximations of Laplace Solutions of Dirichlet, Neuman and mixed type problems. Finite element methods: Linear, triangular elements and rectangular elements.

Recommended Books:

1. M. K. Jain, S.R.K. Iyenger and R. K. Jain: Computational Methods for Partial differential equations, Wiley Eastern, 1994.
2. M. K. Jain, Numerical Solution Differential Equation, 2nd Edition, Wiley Eastern.
3. S. S. Sastry, Introductory Methods of Numerical analysis, Prentice-Hall of India, 2002.
4. D .V. Griffiths and I. M. Smith, Numerical Methods of Engineers, Oxford University Press, 1003.
5. C. F. General and P.O. Wheatley: Applied Numerical Analysis, Addison-Wiley, 1998.
6. B. S Grawal: Higher Engineering Mathematics , Khanna Publication.
7. J. N. Reddy: Introduction to Finite Element Method

Paper IV - Advanced Topology (MAT-307) **Total credit-5**

Unit-1

Characterization of connected sets in terms of open sets and closed sets. Closure of a connected set. Union of connected sets.Connected sets in R. Continuity of a function and connectedness. Components and partition of space. Path connected space.

Unit-2

Inadequacy of sequential convergence. Directed sets, nets and subnets and their examples Convergence of a net, charaterisation of open sets, closed sets, closure, cluster point and limit point of a set in terms of net convergence. Hausdorffness and continuity of a function in terms of nets.

Unit-3

Definition of filter and its examples. Neighborhood filter. Comparison of filters. Filter base and subbase. Convergence of a filter. Ultrafilters. Continuous functions and filters.Net based on filter and filter based on net. Quotient topology, quotient space, quotient map, quotient space X/R, Finite product space, projection mapping.

Unit-4

Tychonoff product topology in terms standard subbase and its characterizations in terms of projection maps, continuous functions, Product of T0,T1,T2, spaces. Connectedness and compactness, first and second countability for product spaces. Homotopy of paths.

Books Recommended:

1. George F. Simmons : Introduction to Topology and Modern Analysis, Mc Graw-Hill Book Company 1963.

2. J.L. Kelley : General Topology, Van Nostrand, Reinhold Co., New York 1995.

3. K.D. Joshi : Introduction to General Topology, Wiley Eastern Ltd., 1983.

4. James R Munkres : Topology, Prentice Hall of India Pvt. Ltd., New Delhi, 2000.

5. S. Willard : General Topology Addison-Wesley, Reading, 1970.

Paper IV - Hydro Dynamics (MAT-308) **Total Credit-5**

Unit-I

Lagrange's Stream function. Irrotational motion in two-dimensions. Complex velocity potential. Two dimensional Sources and sinks. Complex potential due to a source. Doublets. Complex potential for doublets. Image. Image of a source and doublets in a circle.

Unit-II

Milne-Thomson circle theorem. Theorem of Blasius. General motion of the cylinder. Motion of a circular cylinder. The motion in the case of a liquid streaming past a fixed circular cylinder. Initial motion between two coaxial cylinders.

Unit-III

Kinetic energy of liquid. Flow and circulation. Motion of elliptic cylinders. Joukowski transformation. Streaming past a fixed elliptic cylinder. Velocity potential and stream function in case of elliptic cylinders. Circulation about an elliptic cylinder.

Unit-IV

Motion of a sphere through a liquid. Liquid streaming past a fixed sphere. Problem of initial motion of sphere. Stoke's stream function. Irrotational motion. Vortex motion. Vortex lines. Kelvin's proof of permanence. Motion due to circular and rectilinear vortices.

Books Recommended:

1. J.K. Goyal and K.P. Gupta: Fluid Dynamics, Pragati Prakashan, Meerut, 2017

2. N. Curle and H. J. Davis: Modern Fluid Dynamics, D. Van Nostrand Company Ltd. London, 1968.

3. B.G. Verma: Hydrodynamics, Pragati Prakashan, Meerut, 1995.

4. G.K. Batchelor: An Introduction to Fluid Dynamics, Cambridge University Press, Cambridge, 2000.

Paper V- Discrete Mathematics (MAT-309) **Total Credit-5**

Unit 1:

Semigroups & Monoids: Definition and examples of Semigroups and Monoids. Homomorphism of Semigroups and Monoids. Congruence relation and Quotient Semigroups. Subsemigroup and Submonoids. Direct products. Basic homomorphism theorem.

UnitII:

Lattices: Lattices as partially ordered sets. Their properties. Lattices as Algebraic Systems. Sublattices. Direct products and Homomorphisms. Some Special Lattices e.g., Complete, Complemented and Distributive Lattices.

UnitIII:

Boolean Algebras: Boolean Algebras as Lattices, Various Boolean Identities. The Switching Algebra example. Subalgebras. Direct Products and Homomorphisms. Join-irreducible elements, Atoms and Minterms. Boolean Forms and their Euivalence.

UnitIV:

Graph Theory: Definition of Graphs, Paths, Circuits, Cycles & Subgraphs. Induced Subgraphs. Degree of a vertex. Connectivity. Planar graphs and their properties. Trees. Euler's Formula for connected planar graphs.

Books Recommended:-

1. C.L. Liu: Elements of Discrete Mathematics (Second Edition), McGraw Hill,

International Edition, Computer Science Series, 1986.

2. J.P. Tremblay & R. Manohar: Discrete Mathematical Structures with Applications to

Computer Science, McGraw-Hill Book Co., 1997.

3. N. Dew. Graph Theory with Application to Engineering and Computer Sciences,

Prentice Hall of India.

Paper V- Mathematical Modelling (MAT-310) **Total Credit-5**

Unit-I

Need, techniques, classification and simple illustrations of mathematical modelling. Limitations of mathematical modelling, Linear and Non-linear Growth and Decay models. Compartment models. Some techniques for analyzing ordinary differential equation mathematical models.

Unit-II

Continuous Models for interacting Population: Interaction between species: two species models, definition of stability, community matrix approach, Qualitative behavior of the community matrix, Lotka-Volterra model prey predator model, Models for mutualism and competition among the species.

Unit-III

Mathematical modelling in epidemiology, basic concepts, SI model, SIS model with constant coefficient, SIS model when coefficients are function of time, SIS model with constant number of carriers, General deterministic model with removal (Kermack McKendrik model), Epidemic model with vaccination.

Unit-IV

Some simple drug distribution problems, mathematical modelling in pharmacokinetics, the distribution of metabolites in the body, physiological application of the two compartment model, mathematical modeling of drug effects- a more general approach.

Books Recommended:

1. J.N. Kapur: Mathematical Modelling, New Age International (P) Limited, New Delhi.

2. Zafar Ahsan : Differential Equations and Their Applications, PH I learning Private Limited, New Delhi.

3. J. Mazumdar: An Introduction to Mathematical Physiology and Biology, Cambridge University Press.

4. Nicholas F. Britton: Essential Mathematical Biology, Springer.

Paper IV- Complex Manifolds (MAT-311) **Total Credit-5**

Unit-I

Almost Complex Manifolds: Elementary notions, Nijenhuis tensor Eigen values of F, Integrability conditions, Contravariant and covariant analytic vectors, F-connection, half symmetric connection.

Unit-II

Almost Hermit Manifolds: Definition, Almost analytic vector fields. Curvature tensor. Linear connections.

Unit-III

Kaehler Manifolds: Definition. Curvature tensor. Affine connection. Properties of projective, conformal, concircular and conharmonic curvature tensors. Contravariant almost analytic vector

Unit-IV

NearlyKaehler Manifolds: Introduction, Curvature identities, almost analytic vectors.

Books Recommended:

1. R.S. Mishra: Structure on differentiable manifold and their application, ChandramaPrakashan, Allahabad, 1984.
2. K. Yano and M. Kon: Structures of Manifolds, World Scientific Publishing Co. Pvt. Ltd., 1984.
3. U.C.De and A.A.Shaaikh, Complex and Contact Manifolds, Narosa Publishing House, New Delhi 2009.

Paper V- Riemannian Geometry (MAT-312) **Total Credit-5**

Unit-1

Unit normal. Generalised convariant differentiation. Gauss's formulae. Curvature of a curve in a hypersurface. Normal curvature. Mean curvature. Principal normal curvature. Lines of curvature. Conjugate and asymptotic directions. Tensor derivative of the unit normal. Gauss characteristic equation and Mainardi-Codazzi equations. Totally geodesic hypersurfaces.

Unit-II

Unit normals. Gauss's formulae. Change from one set of normals to another. Curvature of a curve in subspace. Conjugate and asymptotic directions. Generalisation of Dupin's theorem. Derived vector of a unit normal. Lines of curvature for a given normal.

Unit-III

Infinitesimal transformation. The notion of Lie derivative. Lie derivative of metric tensor and connection. Motion and affine motion in Riemannian spaces.

Unit-IV

Hyperplanes. Hyperspheres. Central quadric hypersurfaces. Reciprocal quadric hypersurfaces. Conjugate radii. Any hypersurface in Euclidean spaces. Riemannian curvature of a hypershpere. Geodesics in a space of positive constant curvature. (1credit)

Books Recommended:

1. C.E. Weatherburn: An Introduction to Riemannian Geometry and the Tensor Calculus, Cambridge University Press, 1966.
2. K. Yano: The Theory of Lie Derivatives an its Applications, North Holland Publishing Company, Amsterdam,1957.
3. R. S. Mishra: A Course in Tensors with Applications to Riemannian Geometry, Pothishala (Pvt.) Ltd., 1965.

Paper V - Magneto Hydrodynamics (MAT-313) **Total Credit- 5**

Unit I:

Maxwell equations. Electromagnetic field in a conductor. MHD approximations. Rate of flow of charge. Important MHD parameters. Diffusion of magnetic field. Frozen-in-fields. Integral of magnetic field equation. Analogy of magnetic field with vorticity

Unit II:

Alfven theorem. Lorentz force and its transformations. Magnetic energy. Poynting vector theorems. Basic equations of in viscid and viscous magnetohydrodynamics. Energy conservation law.

Unit III:

Alfven waves. MHD waves in a compressible fluid. Equi-partition of energy of Alfven waves. MHD boundary conditions. Equations of incompressible MHD flow.

Unit IV:

Parallel steady flow. Steady parallel flow in a conservative field of force. One-dimensional steady viscous MHD flow. Hartmann flow. Couette flow.

Books Recommended:

1. Alan Jeffery: Magnetohydrodynamics, Oliver and Boyd Ltd., Edinburgh, 1966.
2. F. Chorlton: Text Book on Fluid Dynamics, C.B.S. Publishers, Delhi,1985.
3. S.I. Pai: Magnetohydrodynamics and Plasma Dynamics, Springer-Verlag,1962.
4. P. A. Davidson: Introduction to Magnetohydrodynamics, Cambridge University Press, U.K., 2017.

M.A/M.Sc. Fourth Semester Based on CBCS (Mathematics)

Paper I - Measure Theory (MAT-401) **Total Credit-5**

Unit I:

Lebesgue's outer measure and its properties. Length of an interval and Lebesgue outer measure. Lebesgue measurable sets in R and σ-algebra of Lebesgue measurable sets in R Lebesgue measurability of open sets, closed sets and Borel sets. Labesgue measure on R. Example of a Non-Lebesgue measurable set. Cantor's set and its Labesgue measure.General outer measure . Caratheodory's definition of measurable sets. σ-algebra of measurable sets.

Unit II:

Definition of a measure. Measurable space and a measure space.Definition of a measurable function. Equivalent conditions for measurable function. Sum and product of measurable functions. Composition of a measurable and a continuous function.Sequences of measurable functions. Measurability of supremum function, infimun function, limit superior function, limit inferior function and limit function.

Unit III:.

Simple measurable functions and their properties. A non-negative measurable function as the limit of a sequence of non-negative simple measurable functions. Concept of almost everywhere (a.e.). Lebesgue theorem.Convergence in Measure and its properties. F. Riesz theorem and Egorov theorem. Convergence almost everywhere, almost uniform convergence and their inter-relations.

Unit IV:

Lebesgue Integration of a simple measurable function on R and its properties. Lebesgue Integration of a bounded measurable function on a set E with finite Lebesgue measure, i.e. $\lambda(E) < \infty$ and its properties. Bounded convergence theorem, Fatou's lemma, Lebesgue monotone convergence theorem, Lebesgue dominated convergence theorem, Lebesgue integration and Riemann integration. Integration on a measure space. Lebesgue integral of general measurable function and its properties.

Books Recommended:-:

1. Walter Rudin, Principle of Mathematical Analysis (3rd edition) McGraw-Hill Kogakusha, International Student Edition, 1976.

2. P. R. Halmos, Measure Theory, Van Nostrand, 1950.

3. G. de Barra, Measure Theory and Integration, Wiley Eastern, 1981.

4. P. K. Jain and V. P. Gupta, Lebesgue Measure and Integration, New Age International, New Delhi, 2000.

5. R. G. Bartle, The Elements of Integration, John Wiley, 1966

Paper II - Hilbert Spaces (MAT-402) **Total Credit-5**

Unit I:

Inner product spaces, their basic properties and examples, Schwartz inequality. Norm induced by inner product, Continuity of inner product, Hilbert spaces and their examples. Parallelogram equality, polarization identity. Characterization of inner product in terms of norm. Separable Hilbert spaces and their examples.

Unit II:

Orthogonal vectors. Orthogonal complement. Projection theorem. Projection operators. Orthogonal sets and their advantage over its linearly independent sets. Complete orthonormal sets. Bessel's generalized inequality. Parseval's Relation

Unit III:

Grahm-Schmidt orthogonalization process. Fourier series representation.Bounded linear functionals on Hilbert spaces. Riesz-Frechet representation theorem. Dual spaces. Inner product structure of dual spaces. Reflexivity of Hilbert spaces.

Unit IV:

Hilbert adjoint operators. Shift operators. Special cases of Hilbert adjoint operoters self adjoint operators, positive operator, normal operators, unitary operators. Orthogonal projection operators. Eigen Values of Linear Operator. Spectrum of a Bounded Linear Operator. Spectral properties of bounded linear operators.

Books Recommended:-

1 P.K. Jain, O.P. Ahuja and K. Ahmad: Functional Analysis, New Age International (P) Ltd. and Wiley Eastern Ltd., New Delhi, 1997.
2 B. Choudhary and S. Nanda: Functional Analysis with Applications, Wiley Eastern Ltd., 1989.
3 I.J Maddox: Functional Analysis, Cambridge University Press (1970).
4 B.V.Limaye: Functional Analysis,New Age International Publications, New Delhi.
5 K. Chandrashekhara Rao. Functional Analysis, Narosa Publishing House, New Delhi
6 W.Rudin: Functional Analysis, TMH, New Delhi
7 H.K.Pathak: Functional Analysis with Applications, Siksha Sahitya Prakashan, Merru

Paper III - Analytical Dynamics (MAT-403) **Total Credit-5**

Unit I:

Classification of dynamical systems, generalized coordinates, Holonomic and non holonomic systems, Kinetic energy, Generalized components of momentum, Generalized
Components of the effective and applied forces, Lagrange's equations, Some Examples on Lagrange's equations, Energy equation from Lagrange's equation, Reciprocal relations, Ignoration of coordinates, The Routhian function, Lagrange's equation for impulsive motion, Euler's equation from Lagrange's equation.

Unit II:

Small oscillations, Lagrange's equation of small oscillations. Lagrange's determinants, Normal modes and normal coordinates and their stationary properties.

Unit III:

Hamilton's equations of motion. Applications of Hamiltonian method, Action, Hamilton's principle, Principle of least action, Hamilton-Jacobi equation, Hamilton Jacobi theorem.

Unit IV:

Canonical transformations, conditions of canonicality, cyclic relations, Generating function, Phase space, Bilinear invariants, Poisson brackets, Lagrange brackets. Invariance of Lagrange brackets and Poisson brackets under canonical transformations.

Books Recommended:-

1. S.L. Loney: An Elementary Treatise on the Dynamics of a Particle and a Rigid Body,Macmillan India Ltd., 1982.
2. A.S. Ramsey: Dynamics part-II, The English Language Book Society and Cambridge University Press, 1972.
3. J.L. Synge and B.A. Griffith: Principles of Mechanics, McGraw Hill International Book company, 1982
4. P.P. Gupta, G.S. Malik: Rigid Dynamics I, Krishna Prakashan Media (P) Ltd.2008.

5.Kumar, Generalized Motion of Rigid Body, Narosa Publishing House, New Delhi.

Paper IV - Fixed Point Theory and its Applications (MAT-404) **Total Credit-5**

Unit I:

Background of Metrical fixed point theory, Fixed Points, Uniformly convex, strictly convex and reflexive Banach spaces, Lipschitzian and contraction mapping, Banach's contraction principle, Application to Volterra and Fredholm integral equations, Caristi's fixed point theorem.

Unit II:

Nonexpansive, asymptotically nonexpansive and quasinonexpansive mappings and Fixed Points, Fixed point theorems for nonexpansive mappings, Nonexpansive operators in Banach spaces satisfying Opial's conditions, The demiclosedness principle.

Unit III:

Brouwer's fixed point theorem, Schauder's fixed point theorem, Measure of Non- Compactness, Condensing map, Fixed points for condensing maps, Strict convexity,Uniform convexity,The modulus of convexity and normal structure, Smoothness, retraction map, Sadovskii's fixed point theorem, Introduction of Set-valued mappings, Set-valued contraction map, Housdroff metric, Nadler's fixed point theorem.

Unit IV:

Fixed point iteration procedures: Krasniselskij iteration, Picards iteration, The Mann Iteration, Lipschitzian and Pseudocontractive operators in Hilbert spaces, Strongly pseudocontractive operators in Banach spaces, The Ishikawa iteration, Equivalence between Mann and Ishikawa iterations.

Books Recommended:

1. V. Berinde, Iterative Approximation of Fixed Points, Lecture Notes in Mathematics, No. 1912, Springer, 2007.

2. M. A. Khamsi and W. A. Kirk, An Introduction to Metric Spaces and Fixed Point Theory, John Wiley & Sons, New York, 2001.

3. Sankatha P. Singh, B. Watson and P. Srivastava, Fixed Point Theory and Best Approximation: The KKM-map Principle, Kluwer Academic Publishers, Dordrecht, The Netherlands, 1997.

4. V. I. Istratescu, Fixed Point Theory, An Introduction, D. Reidel Publishing Co., 1981. 5. K. Goebel and W. A. Kirk, Topic in Metric Fixed Point Theory, Cambridge University Press, 1990.

Paper IV - Cosmology (MAT-405) **Total Credit-5**

Unit I:
Static cosmological models, Einstein Universe, de-Sitter Universe, Hubble law, Weyl Postulate

Unit II:
Non-Static cosmological models, Friedmann-Lemaitre-Robertson-Walker (FLRW) cosmological models and its properties, Observable parameters in FRW metric, Particles Horizon, Event Horizon,

Unit III:

Einstein's field equation and dynamics of the universe. Gravitational Collapse, Gravitational Collapse of a Homogeneous Dust ball, Black Holes (Strong Gravitational fields),

UnitIV:
The Kerr metric or the Rotating black Holes, Origin and Evolution of Universe, Creation of matter, C Field Theory, Explosive Creation, Steady State Theory.

Books Recommended:-

1. K. D. Krori : Fundamentals of Special and General Relativity; PHI Publication, 2010.
2. S. R. Roy and Raj Bali : Theory of Relativity; Jaipur Publishing House, 2008.
3. Steven Weinberg : Gravitation and Cosmology : Principles and applications of General Relativity; Wiley Publ.,2005.
4. J. V. Narlikar : An Introductions to Relativity; Cambridge University Press, 2010.
5. I.B. Khriplovich : General Relativity; Springer Science + business media, 2005.

Paper IV - Wavelet Analysis (MAT-406) **Total Credit-5**

UnitI:

Fourier Analysis: Fourier and inverse Fourier transforms, Convolution and delta function, Fourier transform of Square integrable functions. Fourier series,Poisson's Summation formula.

Unit II:

Wavelet Transforms and Time Frequency Analysis: The Gabor Transform.Short-time Fourier transforms and the uncertainity principle. The integralwavelet transforms Dyadic wavelets and inversions.

Unit III:

Frames. Wavelet Series. Scaling Functions and Wavelets: Multi resolution anal-ysis, scaling functions with _nite two scale relations. Direct sum decomposition of $L^2(R)$: Linear phase filtering.

Unit-IV

Compactly supported wavelets, Wavelets and their duals, Orthogonal Wavelets and Wavelet packets, Example of orthogonal Wavelets. Identi_cation of orthogonal two-scale symbols, Construction of Compactly supported orthogonal wavelets, Orthogonal wavelet packets, orthogonal decomposition of wavelet
series.

Recommended Books:

1.C. K. Chui, A First Course in Wavelets, Academic press NY 1996.
2. I. Daubechies, Ten Lectures in Wavelets, Society for Industrial and Ap-plied Maths, 1992.

Paper IV - Hydro Statics (MAT-407) **Total Credit-5**

Unit I:

Fluid Pressure: Equation of pressure, Necessary condition of equilibrium, surface of equal pressure, curves of equal pressure and density, Elastic fluids, Rotating fluids.

Unit II:

Resultant Pressure and Centre of pressure: Formula for Centre of pressure, geometrical position of centre of pressure, locus of centre of pressure, resultant pressure on curved surfaces.

Unit III:

The equilibrium of Floating Bodies: Conditions of equilibrium, Principle of potential energy and Work done, Surface of Buoyancy.

Unit IV:

Stability of Floating Bodies: Meta centre, Conditions of stability, Work done in small displacement, floating vessel containing liquid, Stability in Heterogeneous Liquid.

Books recommended:

1. Bhu Dev Sharma: Hydro – statics, Kedar Nath Ram Nath.
2. M. Ray, H. S. Sharma : A Text Book of Hydro- statics, S. Chand
3. Rahman: Hydrostatics, Savera Publishing House.
4. N. Inoue, M. Nishihara: Hydrostatic Extrusion: Theory and Applications, Springer
5. S.L. Loney: Mechanics and Hydrostatics for beginners, Cambridge University Press

Paper IV - Mathematics for Humanities (MAT-408) **Total Credit-5**

Unit-I

Functions and graphs, Elementary functions, Exponetial functions and Natural Logarithms, Trignometrical functions, Limit and continuity of Functions.

Unit-II

The meaning of derivative, Calculus of derivative, Applications of derivative, Optimization, Exponential Growth and Decay, Linearization of Functions.

Unit-III

Functions of two variables, Graphical representation of functions, Linearization of functions of two variables, Vectors and matrices, System of linear equations, The inverse matrix.

Unit-IV

First order ordinary differential equations, Applications of ordinary differential equation in exponential growth and decay, Solutions and direction fields, Ordinary differential equation with variables seperable. The spread of infectious diseases, Drug dosage.

Books Recommended:

1. **Shaffer Hall:** Differential and Integral calculus with Applications, MEDTECH, Scientific International Pvt. Ldt.
2. **Arun Kumar**: Mathematics for Biologists, Narosa Publising House, New Delhi

Paper V - Information Theory (MAT-409) **Total Credit-5**

Unit I:

Measure of Information-Axiom for a measure of uncertainty. The Shannon entropy and its properties. Joint and conditional entropies. Transformation and its properties. Noiseless coding-Ingredients of noiseless coding problem. Uniquely decipherable codes. Necessary and sufficient condition for the existence of instantaneous codes.Construction of optimal codes.

Unit II:

Discrete Memoryless Channel-Classification of channels. Information processed by a channel. Calculation of channel capacity. Decoding schemes. The ideal observer .The fundamental theorem of information theory and its strong and weak converses. Continuous Channels-The time-discrete Gaussian channel. Uncertainty of an absolutely continuous variable. The converse of the coding theorem for time-discrete Gassian channel. The time-continuous Gaussian channel. Band-limited channels.

Unit III:

Some imuitive properties of a measure of entropy Symmetric, normalization, expansibility, boundedness, recursivity, maximality,stability, additivity, subadditivity, nonnegativity, continuity, branching etc. and interconnections among them. Axiomatic charachterization of the Shannon entropy due to Shannon and Fadeev. Information functions, the fundamental equation of information, information functions continuous at the origin, nonnegative bounded information functions, measurable information functionsand entropy. Axiomatic charachterisations of the Shannon entropy due to Tverberg and Leo.

Unit IV:

The general solution of fundamental equation of equation of information. Derivations and their role in the study of information functions. The branching property.Some charechterizations of the Shannon entropy based upon the branching property. Entropies with sum property.The Shannon inequality.Subadditive, additive entropies. The Renji entropies. Entropies and mean values. Average entropies and their equality, optimal coding and the Renji entropies.Charechterization of some measures of average code length.

Books Recommended:-

1.R. Ash, Information Theory, Interscience Publishers, New York, 1965.
2. F.M. Reza, An introduction to Information Theory, MacGraw-Hill Book Company Inc., 1961.
3. J. Aczel and Z .Daroczy, On measures of information and their charechterizations, Academic Press, New York.

Paper V - Bio Mathematics (MAT-410) **Total Credit-5**

Unit I:

Introduction, Definition and scope of Bio-Mathematics, Role of Mathematics in Biosciences. Bio-Fluid Dynamics, Human Cardiovascular System and Blood flows, Blood flow through artery with mild stenosis. Two layered flow in a tube with mild stenosis.

Unit II:

Pulsatile flow of blood, analysis and applications of arterial flow dynamics, derivation of aortic Diastolic- Systolic pressure waveforms, Moens-Korteweg expression for pulse wave velocity in an inviscid fluid filled elastic cylindrical arterial tube model, Analysis and applications of left ventricular mechanics, analysis and applications of heart valve vibration.

Unit III:

Human Respiratory System, Gas exchange and air flow in human lungs. Consumption and transport of Oxygen. Weibel's model for flows in human lung airways, Comparison between flows of blood and flows in lung airways.

Unit IV:

Diffusion, Fick's laws of diffusion, Diffusion equation and its solution, Modification of the diffusion equation, Diffusion in artificial kidney, Hemodialyser, Types of Hemodialyser.

Books Recommended:-

1. J.N. Kapur: Mathematical Models in Biology and Medicine, Affiliated East-West Press Pvt. Ltd., New Delhi, 1985.
2. Y.C. Fung: Bio-Mechanics, Springer-Verlag New York Inc., 1990.
3. Stanley E. Charm and George S. Kurland: Blood Flow and Microcirculation, John Wiley & Sons, 1974.
4. S.A. Levin: Frontiers in Mathematical Biology, Springer-Verlag, 1994.
5. S.K. Pundir & R. Pundir : Biomathematics, Pragati Prakashan, 2010.
6. J. Mazumdar: An Introduction to Mathematical Physiology and Biology, Cambridge University Press.

Paper V - Contact Manifolds (MAT-411) **Total Credit 5**

Unit I:

Almost Contact Manifolds: Definition. Eigen values of F. Intergrability conditions of π_m, π_m and π_1. Lie derivative. Normal contact structure. Affinily almost cosymplectic manifold.

Unit II:

Almost Grayan Manifolds: Introduction. D-conformal transformation. Particular affine connections. Almost Sasakian manifold. Quasi-Sasakian manifold.

Unit III:

Sasakian Manifolds: K-contact Riemannian manifold and its properties, Sasakian manifold and its properties. Properties of projective, conformal curvatures in Sasakian manifold.

Unit IV:

Concircular and con- harmonic curvatures in Sasakian manifold. Cosymplectic structure and Nearly Cosymplectic structure. F-structure manifolds: Definitions and some basic properties.

Books Recommended:-:

1. R.S. Mishra: Structure on differentiable manifold and their application, ChandramaPrakashan, Allahabad, 1984.

2. K. Yano and M. Kon: Structures of Manifolds, World Scientific Publishing Co. Pvt. Ltd., 1984

Paper V - Finsler Geometry (MAT-412) **Total Credit-5**

Unit 1:
Finsler metric function. Its properties. Tangent space. Indicatrix. Metric tensor and C-tensor Homogeneity properties of gij and Cijk .

Unit2:

Dual tangent space. Geodesics. δ-differentiation.Partial δ-differentiation. Properties of partial δ-differentiation.

Unit2:

Fundamental postulates of Cartan. Cartan's covariant derivatives and their properties.Geometry of paths. Berwald's covariant derivative and its properties.

Unit2:

Commutation formula resulting from partial δ-differentiation. Other commutation formulae. Three curvature tensors of Cartan. Identities satisfied by curvature tensors including Bianchi identities.

Books Recommended:-

1. H. Rund: The Differential Geometry of Finsler Spaces, Springer-Verlag, 1959.

2. M. Matsumoto: Foundations of Finsler Geometry and special Finsler spaces, Kaiseisha Press, Saikawa, Otsu, 520 Japan, 1986.

Paper V - Mathematics for Life Sciences (MAT-413) **Total Credit-5**

Unit-I

The simple epidemic and SIS diseases, SIR epidemics, SIR endemics: No desease related death including disease related death, eradication and control, Vector-borne diseases, Basic model for macro parasitic diseases.

Unit-II

Modelling AIDS epidemic, Anderson's first model, Anderson's improved model, Interaction of HIV and Immune system, Stages in the course of HIV infection, Treatment of HIV infection, Modelling of HIV immunology, Analysis of treatment of HIV infection.

Unit-III

Tumor modelling, Phenomenological models, Nutrients, Diffusion limited stages, Moving boundary problem, Growth promotors and inhibitors, Vascularizations, Metastasis, Immune system response.

Unit-VI

Human genetics, Basic models for inheritance, Genetic matrices, Hardy-Weinberg law, Correlation between Genetic composition of siblings, Phenotype ratios, Multiple alleles and Apllication to Blood Group, Inheritance of sex linked characterestics, Models for Genetic Improvement: Selection and Mutation.

Books Recommended:

1. **J. Mazumdar**: An Introduction to Mathematical Physiology and Biology, Combridge University Press.
2. **Nicholas F. Britton**: Essential Mathematical Biology, Springer
3. **J. N. Kapur**: Mathematical Models in Biology and Medicine, Affiliated East-west Press Pvt. Ltd., New Delhi.
4. **Fred Brauer, Carlos Castillo-Chavez**: Mathematical Models in Population Biology and Epidemiology, Springer
5. **Matt J. Keeling and Pejman Rohani**: Modelling Infeccious Diseases in Humans and Animals, Princton University Press